

On the ac magnetic susceptibility of spin-chains: solitons in one-dimensional systems

S. Pikin

Shubnikov' Institute of Crystallography RAS, Moscow, Russia

Z. Tomkowicz

Institute of Physics, Jagiellonian University, Krakow, Poland

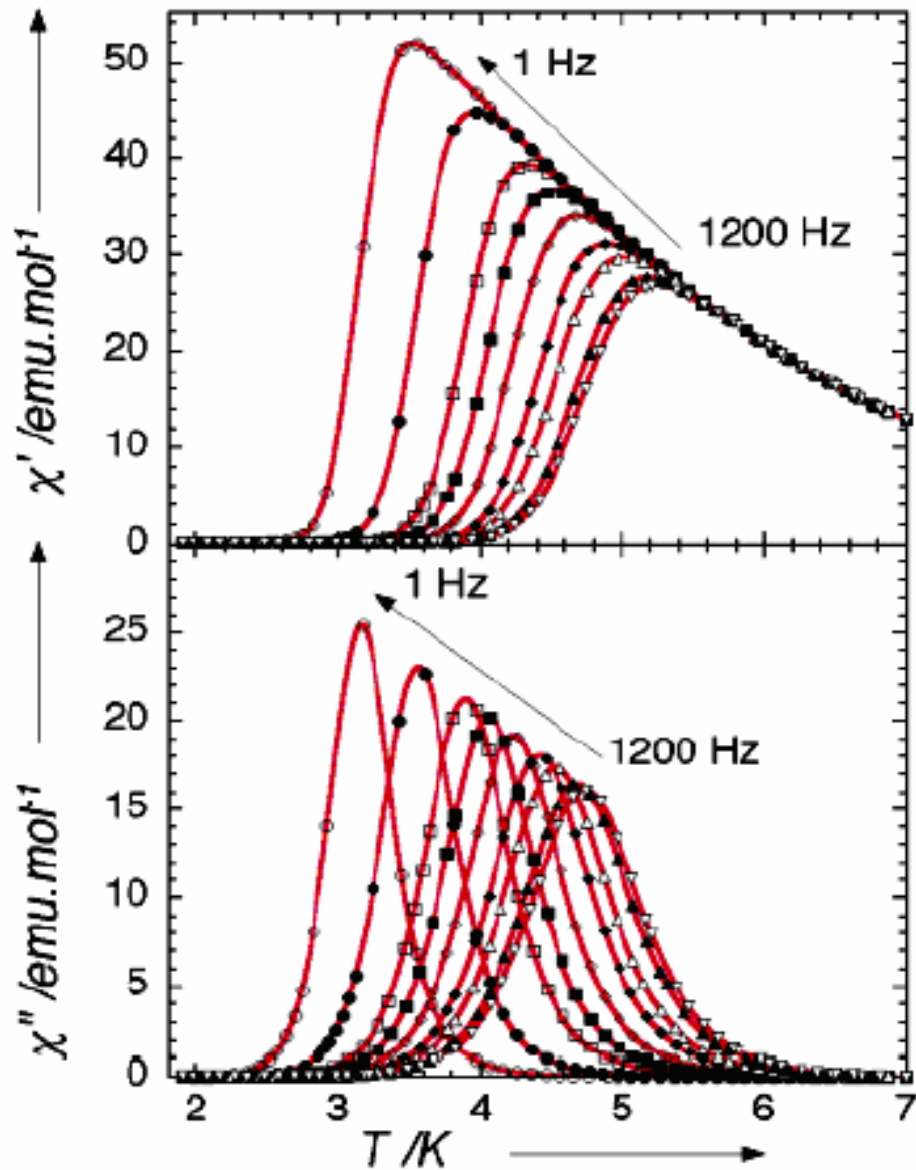
E. Pikina

Institute for Problems of Oil and Gas RAS, Moscow, Russia

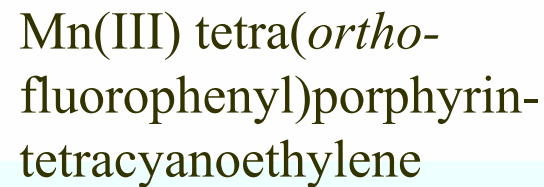
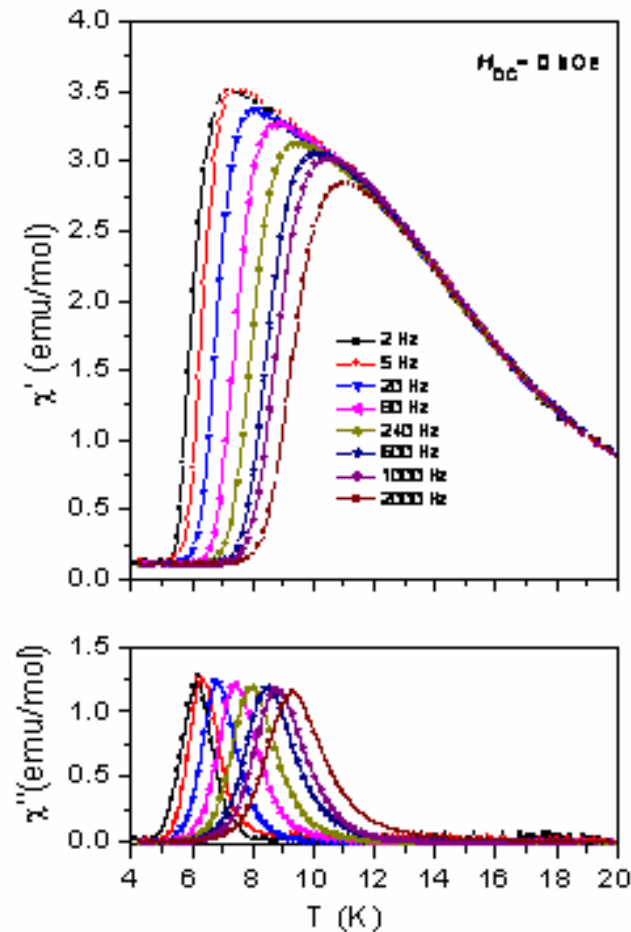
W. Haase

Institut für Physikalische Chemie, Technische Universität
Darmstadt, Germany

Exact solutions show that the perpendicular susceptibility at low temperatures has weak singularities in transverse H at $T = 0$ in reference to the change of J/H [S.A. Pikin and V.M. Tsukernik, Sov. Phys. JETP **23**, 914 (1966)]



H. Miyasaka, R. Clerac, K. Mizushima et al., Inorg. Chem. **42**, 8203(2003)



M. Balanda, M. Rams, S.K. Nayak et al., Phys. Rev. B **74**, 224421 (2006)

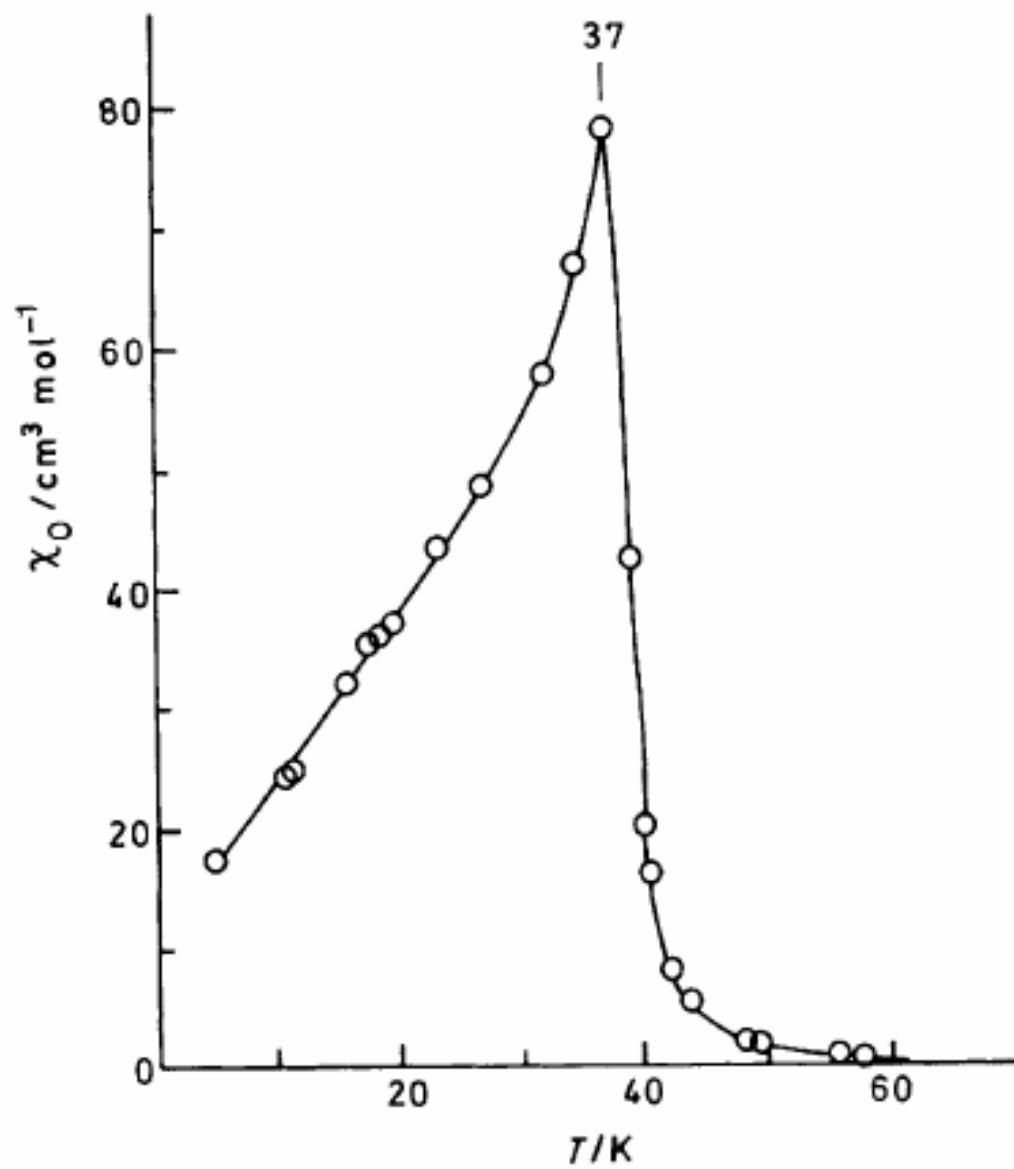


Figure 2. Initial susceptibility of $[\text{NH}_3(\text{CH}_2\text{Ph})]_2[\text{CrCl}_4]$ from 5 to 60 K

Movement of magnetic moment under the action of alternating magnetic field

$$-MH \sin \varphi - U \sin \varphi \cos \varphi + K \frac{\partial^2 \varphi}{\partial z^2} = \gamma \frac{\partial \varphi}{\partial t}$$

$$\tilde{H} = H \cos(\omega t)$$

$$s = \frac{z}{\eta} \quad a = \frac{d}{\eta} \quad \eta = \sqrt{\frac{K}{U}} \quad b = \frac{MH}{\gamma} \equiv \frac{1}{\tau_H}$$

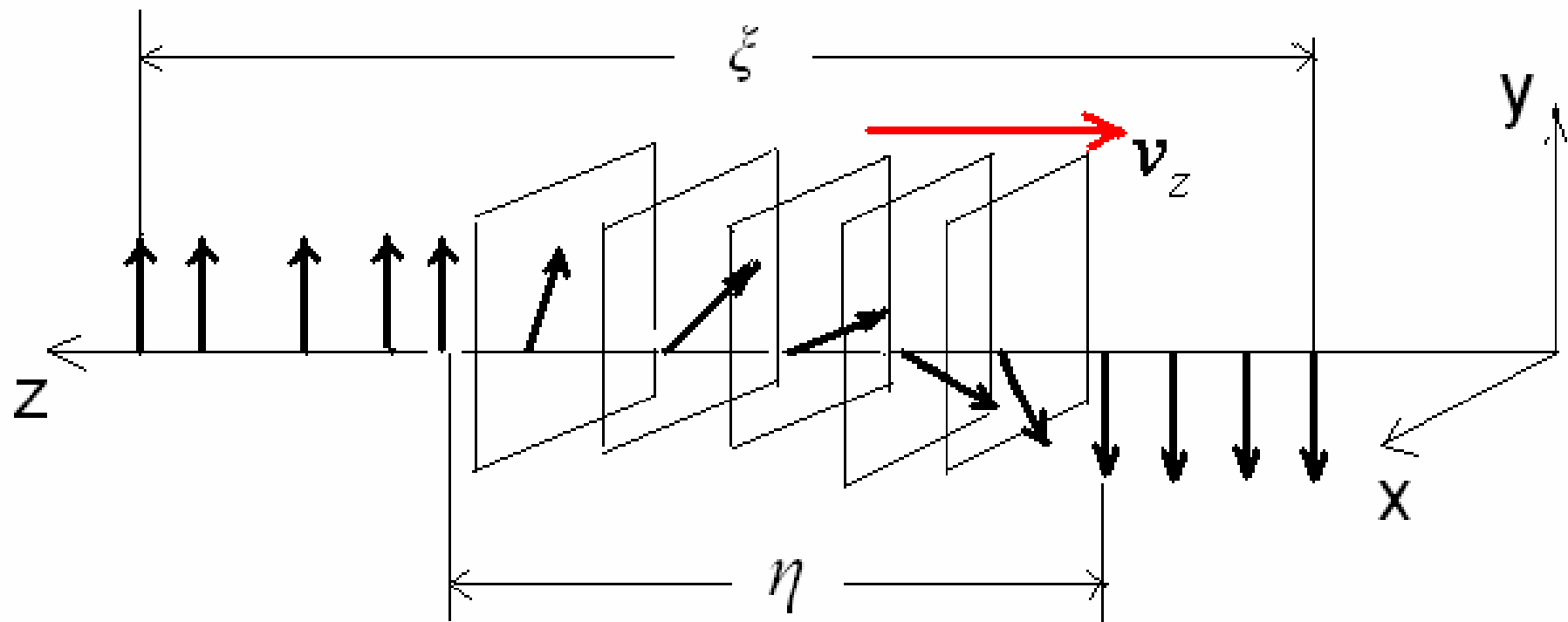
The azimuth rotation of magnetic moment in XY plane

The kink or soliton motion along Z axis

$$\varphi(s, t) = \arctan \left[\frac{1}{\sinh \left(\pm s - s_0 + \frac{b}{\omega} \sin(\omega t) \right)} \right]$$

$\varphi = 0$ and $\varphi = \pi$ at the boundaries, i.e. when value

$$s - s_0 = \frac{z - z_0}{\eta} \quad \text{is much larger than 1}$$

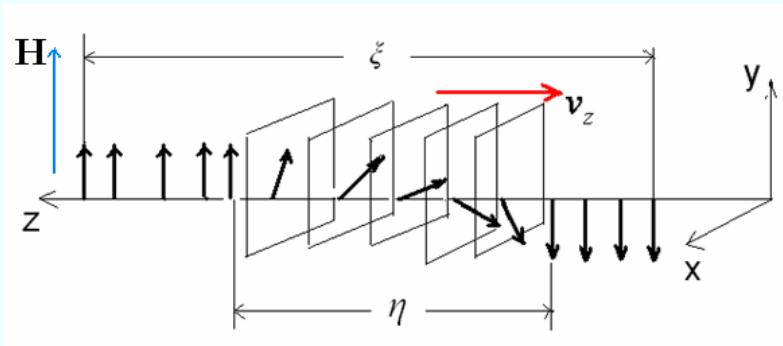


The soliton velocity

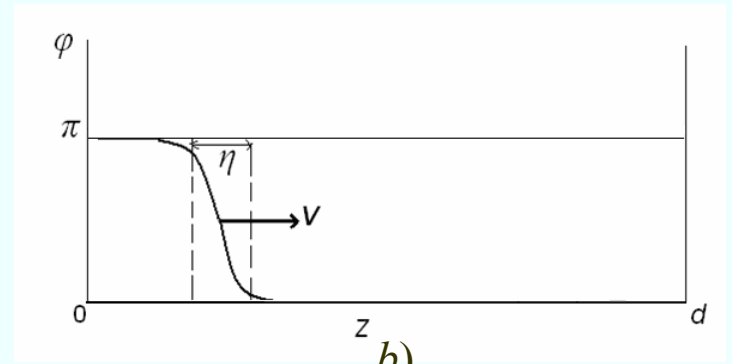
$$v_z = \mp \eta b \cos(\omega t)$$

$$\sin \varphi = \pm \frac{1}{\cosh\left(s + \frac{b}{\omega} \sin(\omega t)\right)}$$

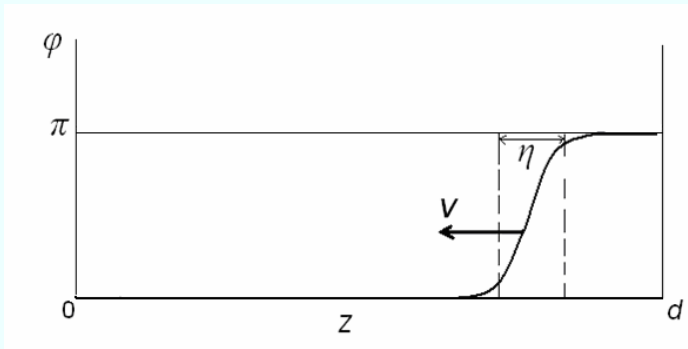
$$\cos \varphi = \tanh\left(s + \frac{b}{\omega} \sin(\omega t)\right)$$



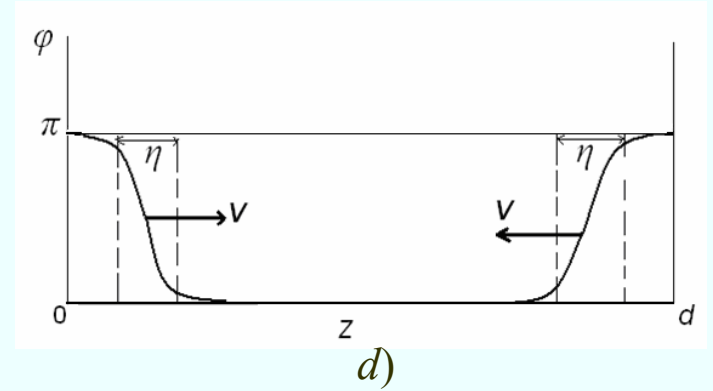
a)



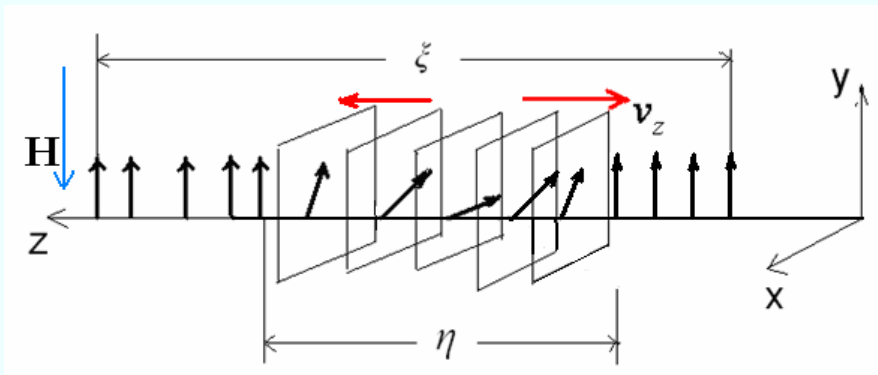
b)



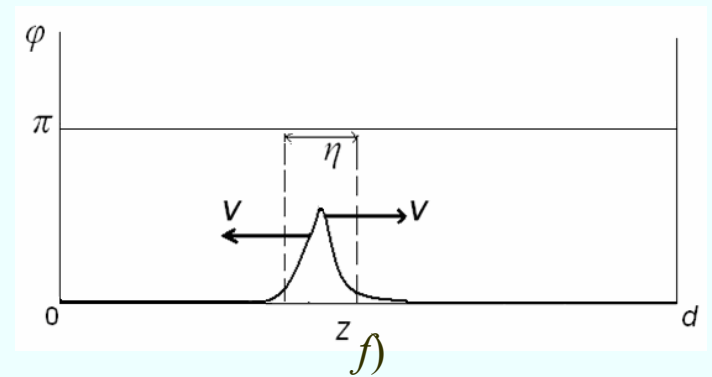
c)



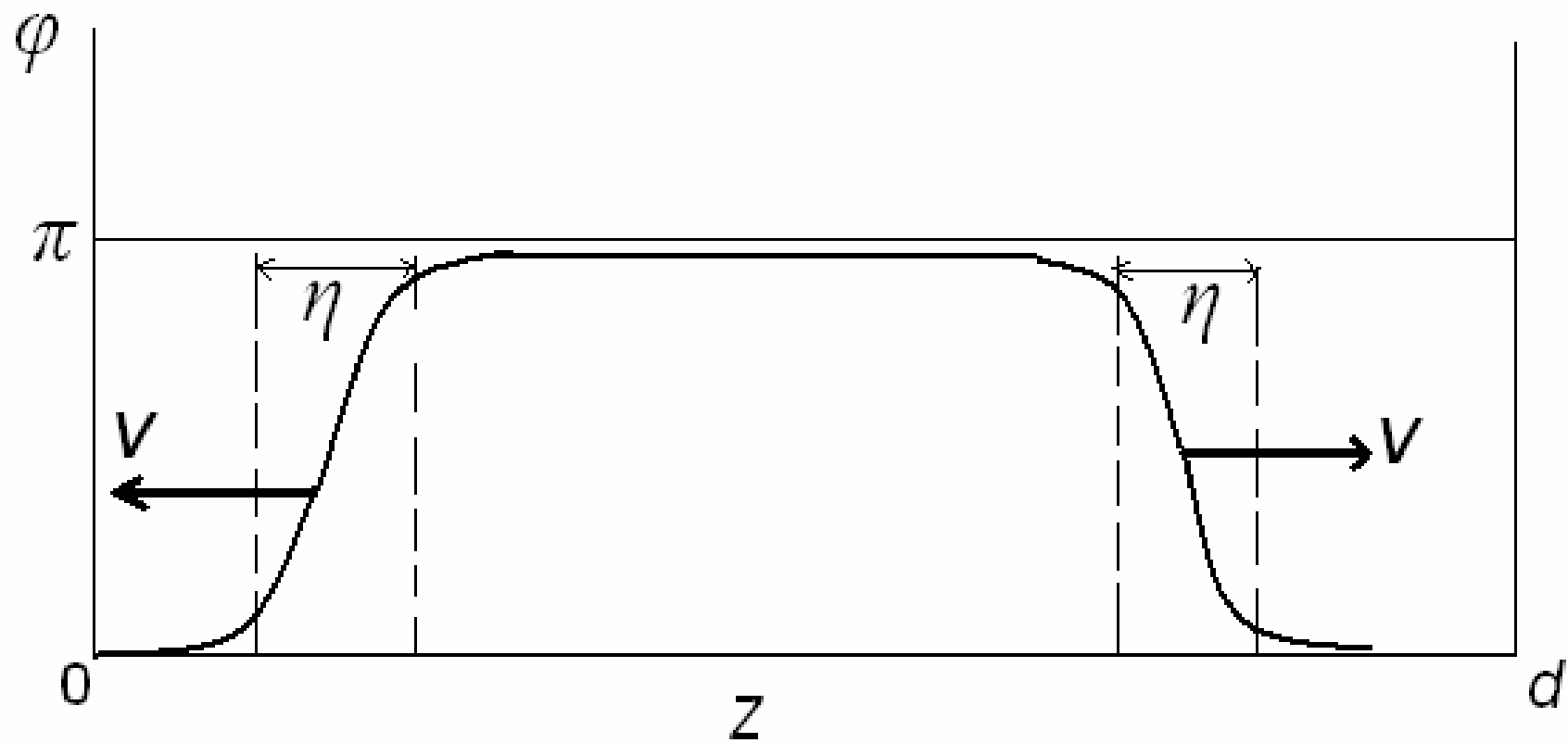
d)



e)



f)



Magnetic susceptibility as the function of temperature and frequency

$$\chi(T, \omega) = \frac{M^2 N}{k_B T} \langle \sin^2 \varphi \rangle \equiv \frac{M^2 N}{2\pi k_B} f(T, \omega)$$

$$f(T, \omega) = \frac{\omega}{T} \int_0^{2\pi/\omega} dt \cdot \frac{1}{d} \int_0^d dz \cdot \sin^2 \varphi(z, t) =$$

$$= \frac{1}{aT} \int_0^{2\pi} \tanh \left[a + \frac{b}{\omega} \sin x \right] dx$$

$$x = \omega t$$

$$m_{eff} = g \sqrt{J(J+1)} \mu_B$$

The factor $m_{eff}^2 N / 2\pi k_B \approx 0.5$ (*emu/mol*)K for the second substance, but for first substances, it is equal approximately 6 (*emu/mol*)K, i.e., 10 times larger as the former.

In fact, $a \sim \xi/\eta$, ξ – correlation length

For n defects per length ξ , the solitons can only move on distance $d = \xi/n$

The upper limit $\chi \sim nf < (2\pi n/Ta)$

Accordingly to the assumption of Glauber, the appearance of kinks has a thermo-activation character.

We shall suppose that the τ_H^{-1} value is the inverse time τ^* for of nucleus formation, $\omega_c \sim 1/\tau^*$, when frequency ω is less than $\omega_c \sim 1/\tau^*$, but $\tau_H^{-1} \sim (\tau^* \omega)^\alpha \omega$ when ω is larger than ω_c . The power index α can be found experimentally. At $\omega \sim \omega_c \sim 1/\tau^*$, τ_H^{-1} becomes of the order $1/\tau^*$.

What is time τ^* ?

$$\tau^* = \tau_0 \exp(E / T)$$

If the time $1/\omega$ is less than the time τ^* , then solitons (as collective motions of spins) cannot arise below a certain blocking temperature T_0 .

We suppose

$$b = \frac{1}{\tau_H(\omega)} \approx \left(\frac{B \tau_0}{T} \right) \omega^{1+\alpha} \exp\left(\frac{E}{T} \right)$$

E – activation energy

When H is less than H_c and $\omega \geq \omega_c$,

Δz interval, were the magnetic moment sharply changes its orientation, becomes to be dependent on ω , and it is less than η .

$$H_c \propto \frac{K}{\mu_B} \cdot \frac{1}{\Delta z^2}$$

$$\Delta z^2(\omega) \propto \frac{D_{orient}}{\eta^2 \omega} \quad \text{accordingly to the diffusion equation}$$

$$H_c \propto \omega$$

$$\text{When } H = H_c \approx \frac{K\eta^2\omega}{\mu_B D_{\text{orient}}}$$

$$\frac{1}{\tau_{H_c}} \propto \frac{H_c^2}{\gamma T} \exp\left(\frac{E}{T}\right) \propto \frac{\omega^2}{\gamma T} \left(\frac{K\eta^2}{\mu_B D}\right)^2 \exp\left(\frac{E}{T}\right)$$

It is supposed that this dependence on ω takes place at $\omega \geq \omega_c$

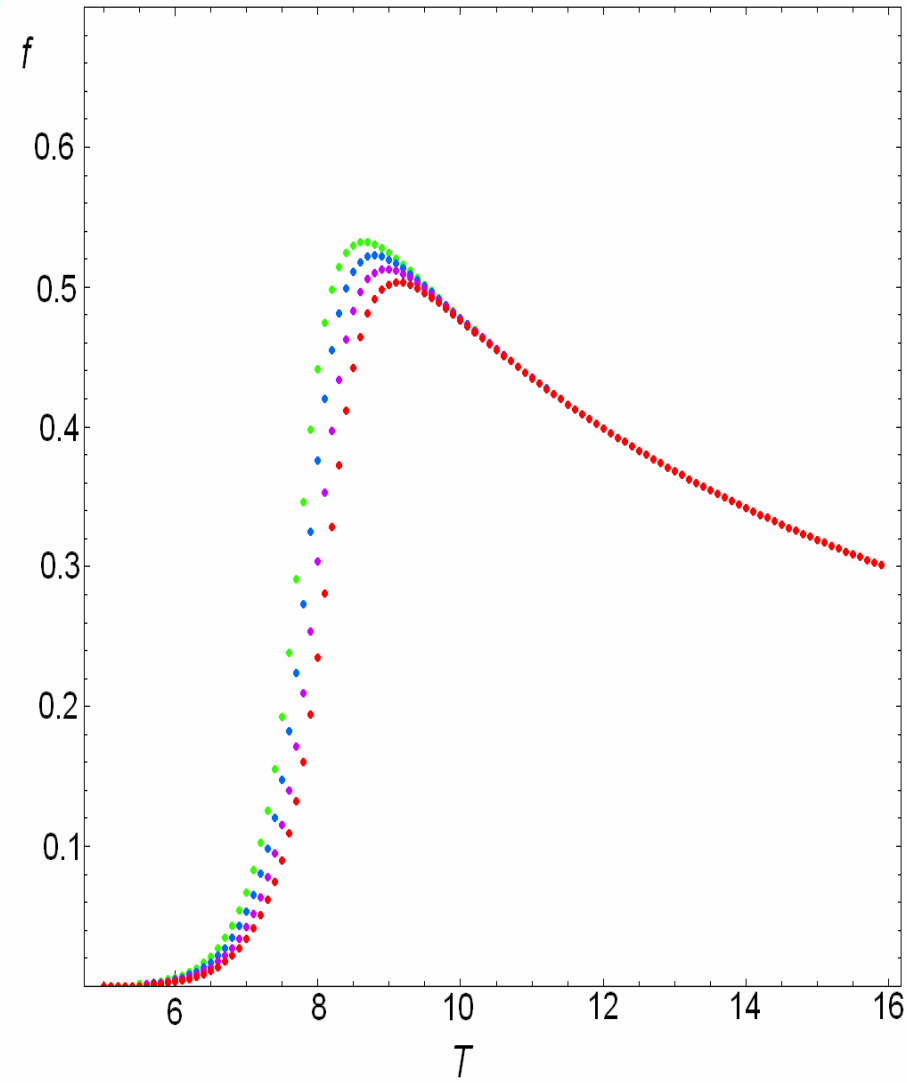
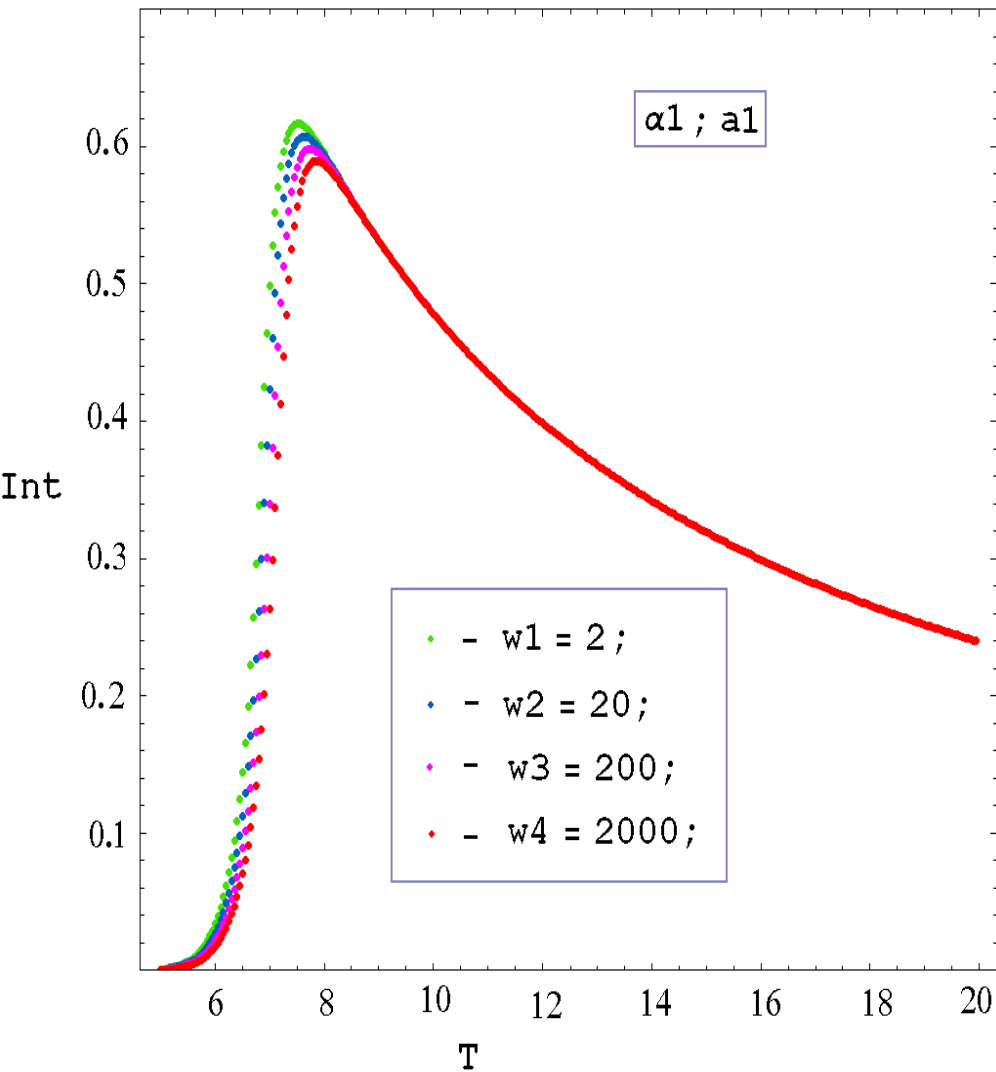
when $H \leq H_c$

Computer simulation

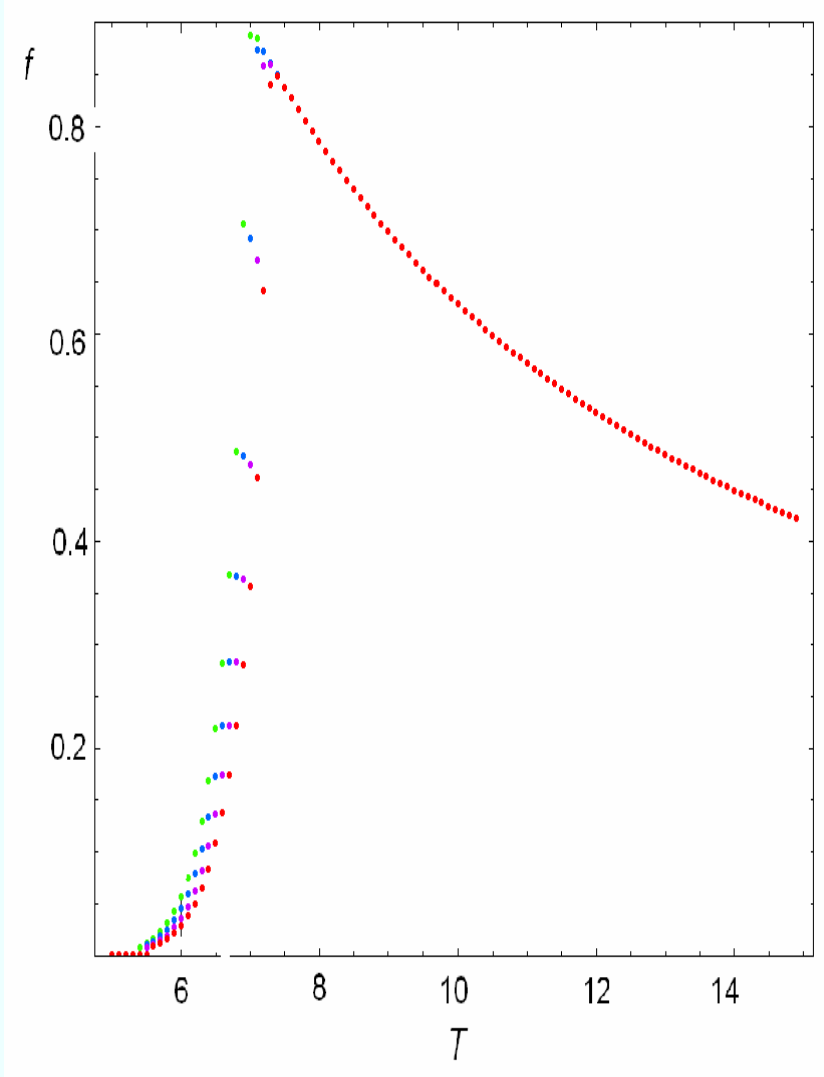
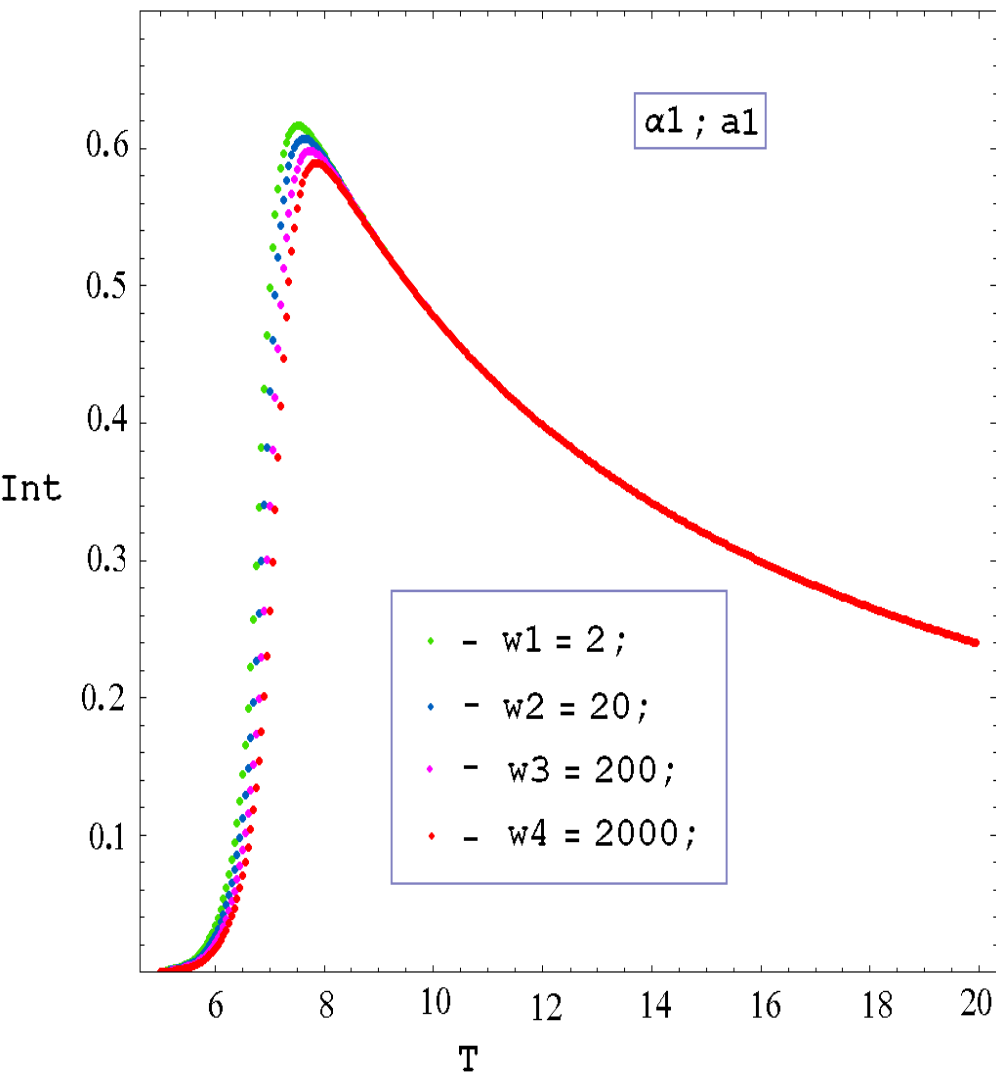
$$f(T, \omega) = \frac{1}{T} \int_0^{2\pi} \tanh \left[2 + \left(\frac{4310}{T} \right) \cdot \omega^\alpha \cdot \exp \left(-22 + \frac{110}{T} \right) \sin x \right] dx$$

At sufficiently high temperatures, all the curves $f(T, \omega)$ turn to *one universal curve* ($\sim 1/T$) for different frequencies.

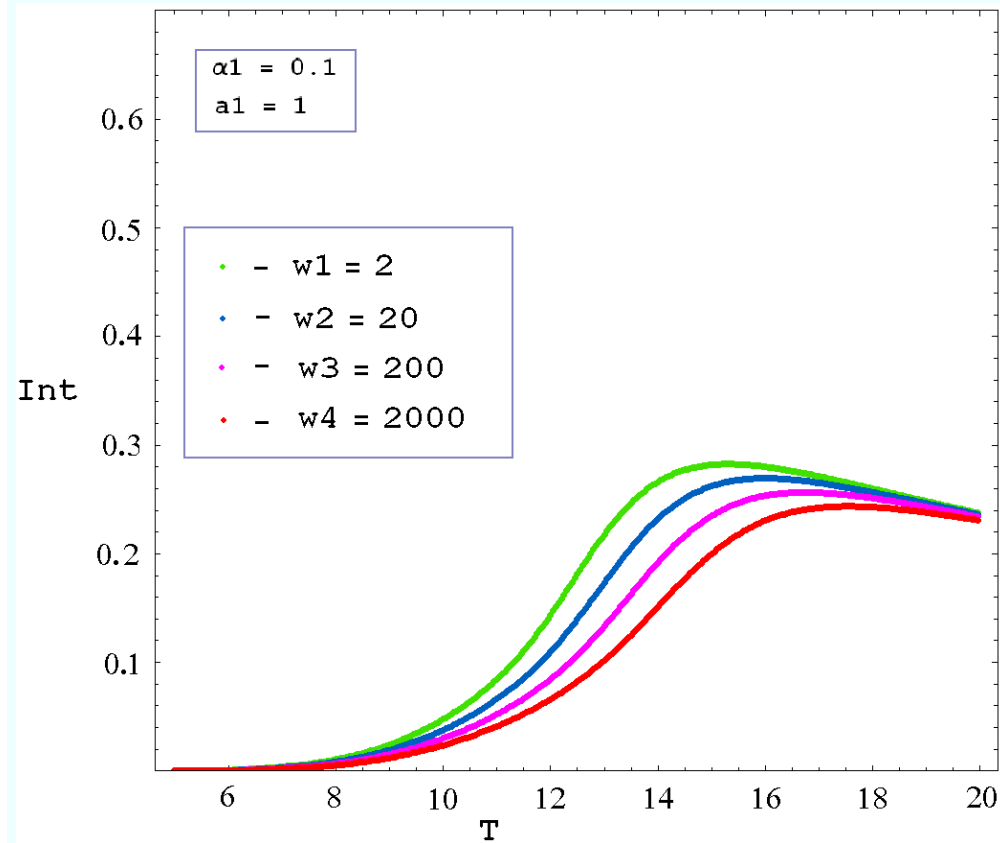
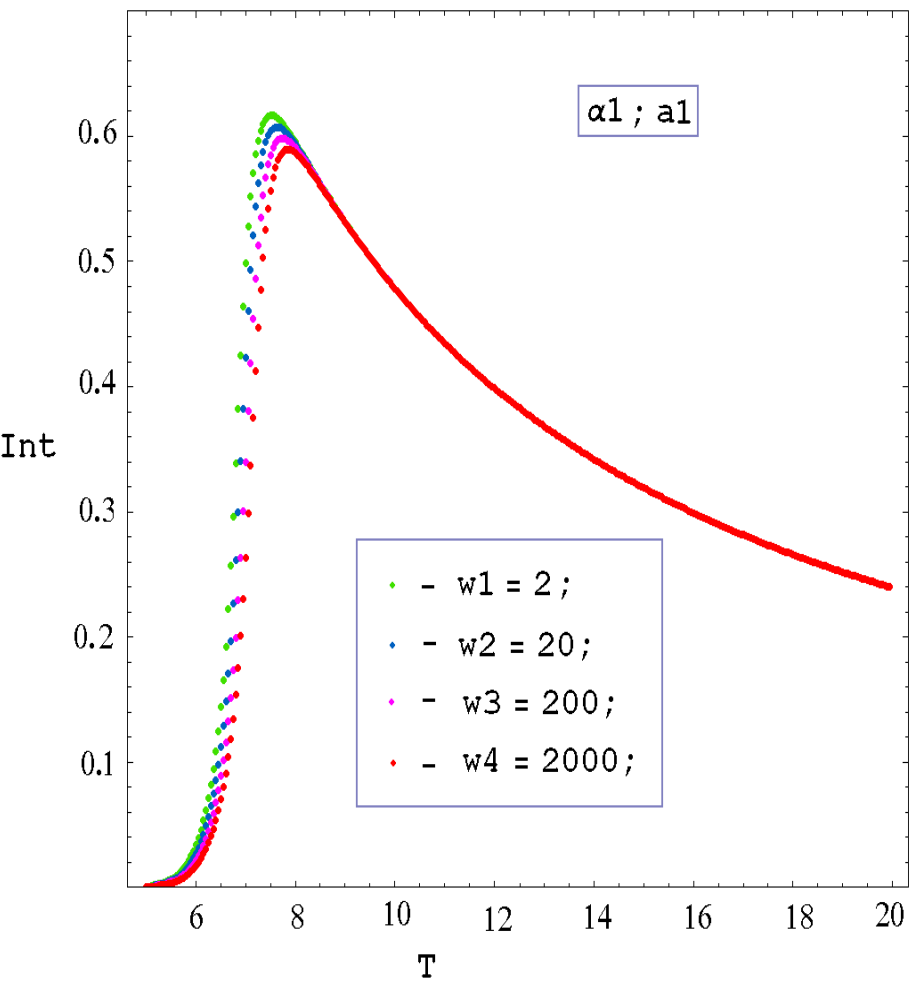
$f_{\max}(\omega) = f(T_0, \omega)$ increases with the increase in *activation energy* E ,
and in ratio a



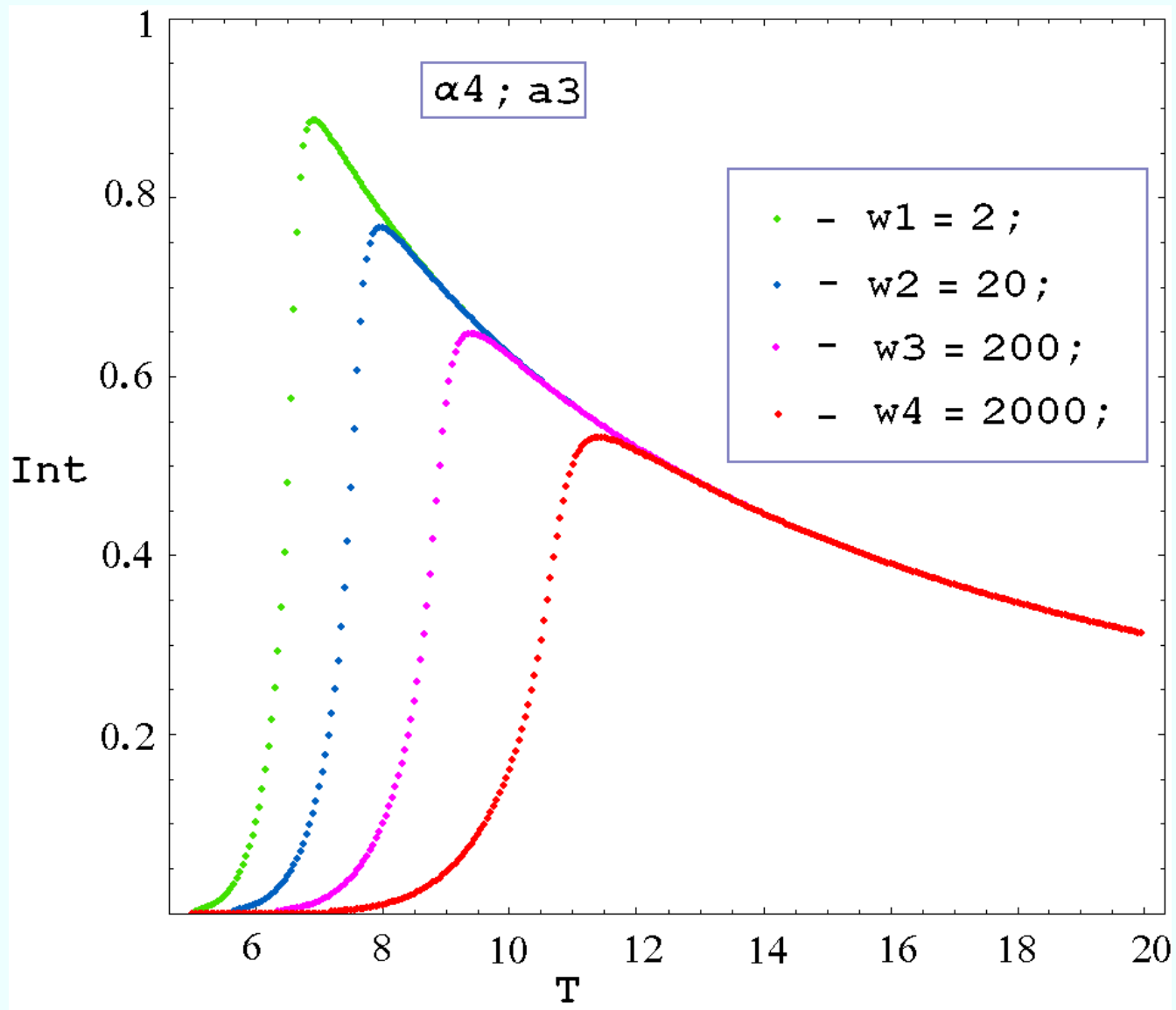
The presence of multiplier $1/T$ in “relaxation frequency” b does not show a strong effect for f , only slightly increasing f .

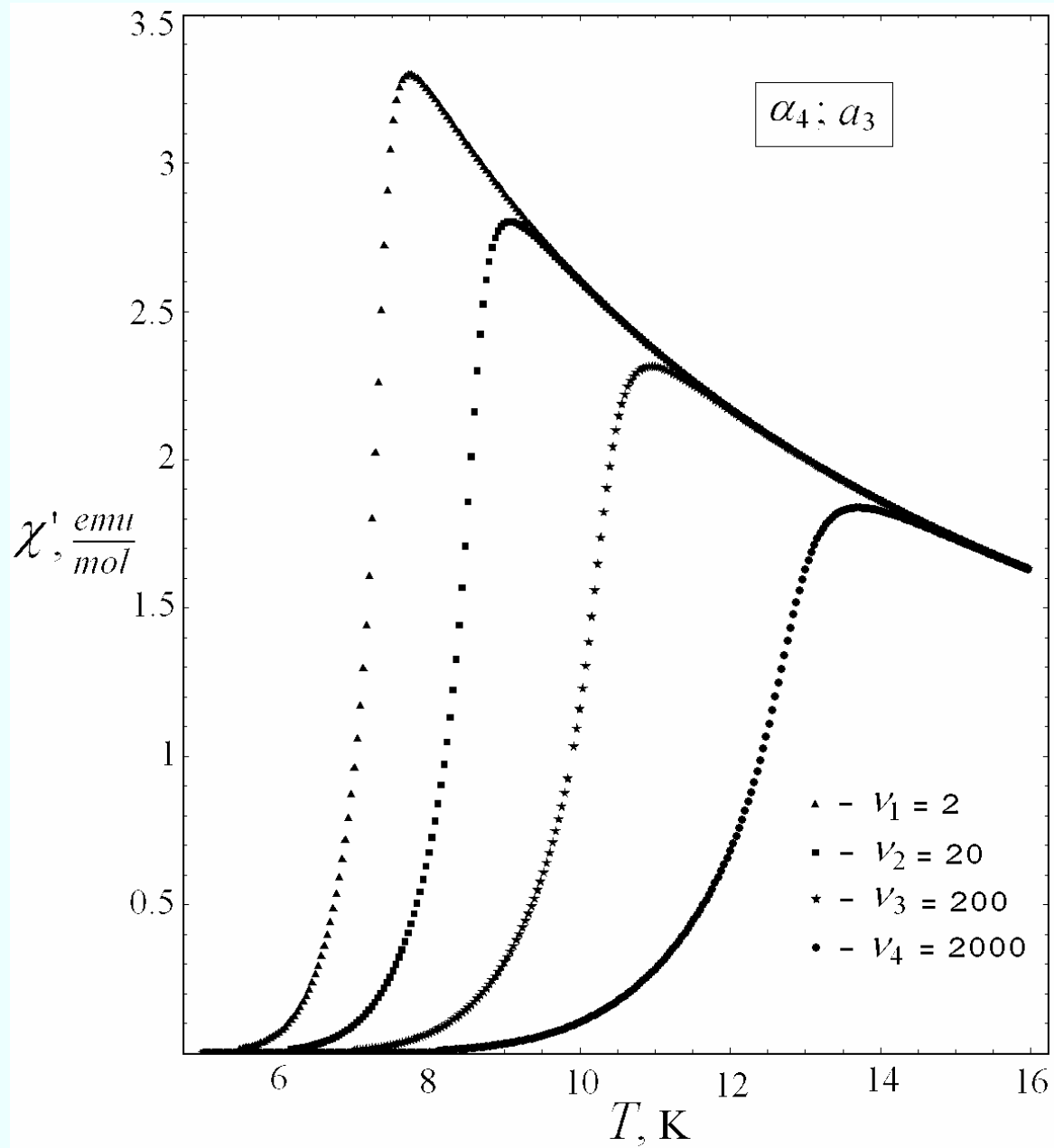


$f_{\max}(\omega) = f(T_0, \omega)$ increases with the increase in ratio a



$f_{\max}(\omega) = f(T_0, \omega)$ increases with the increase in activation energy E





$$\chi'_{\text{experim}} \approx 50 \text{ (emu/mol)K},$$

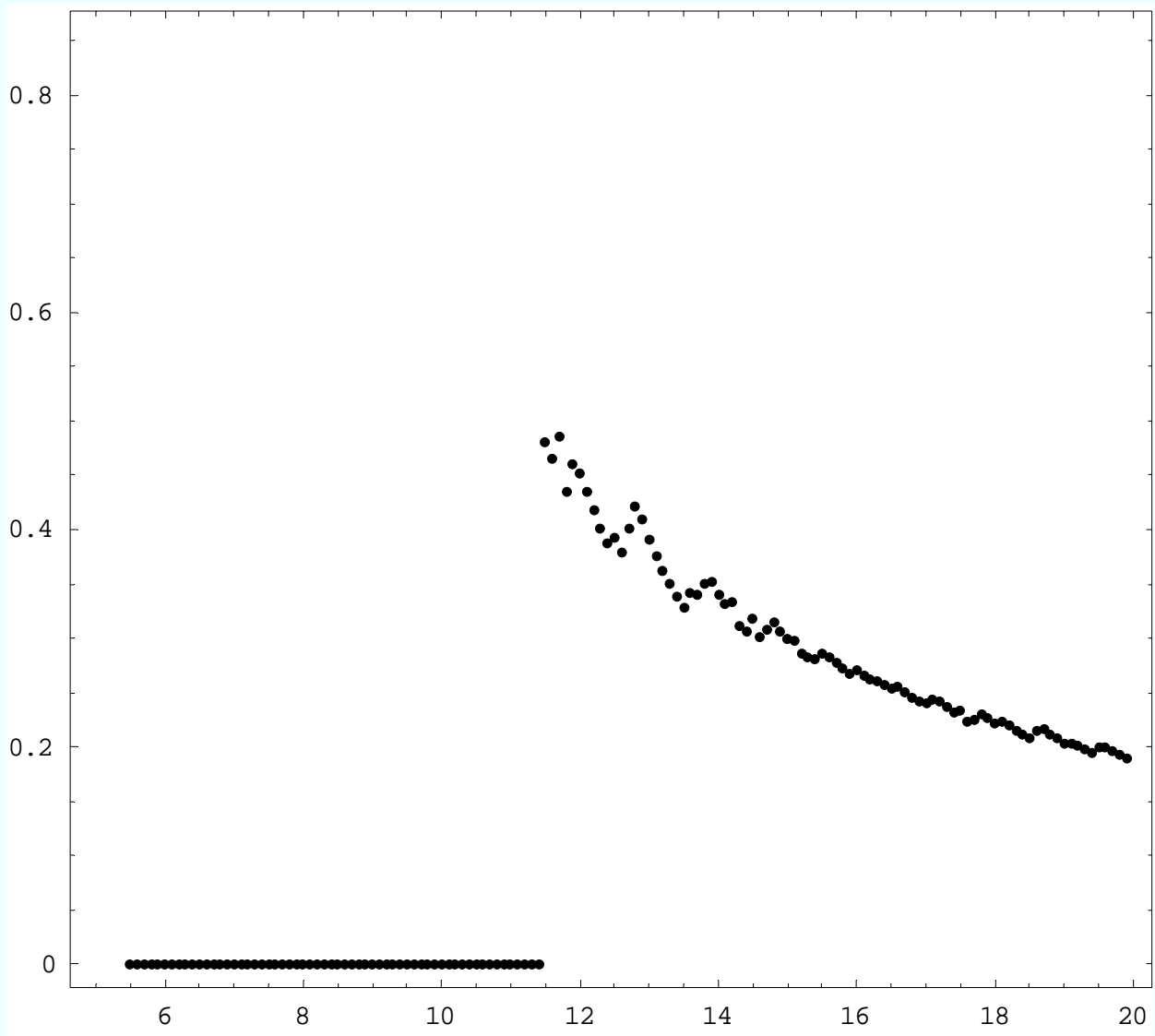
$$m_{\text{eff}}^2 N / 2\pi k_B \approx 6 \text{ emu/mol}, \quad a = 3, \quad f_{\text{max}}(10) \approx 0.9,$$

$$\chi'_{\text{experim}} \approx 3.5 \text{ emu/mol},$$

$$m_{\text{eff}}^2 N / 2\pi k_B \approx 0.5 \text{ (emu/mol)K}, \quad a = 3, \quad f_{\text{max}}(10) \approx 0.9, \text{ i.e.,}$$

$2n \sim 40 \div 60$ solitons can arise and spread simultaneously.

The kinks are sufficiently wide in the considered substances (their width η is 3 – 5 times less than length d).



About the temperature dependence of dc susceptibility χ_{dc}

In an one-dimensional case: some models (see for example the Kadanoff' Gaussian model and Nakamura –Sasada spin chain model) show that parallel susceptibility and correlation length have the same “critical” temperature dependence, i.e.,

$$\chi_{dc} \sim \xi \sim \exp(\Delta/T)$$

The relaxation time for solitons

$$\tau_{relax} \approx \gamma \eta^2 / K$$

i.e., $\tau_{relax} \propto \exp(2\Delta / T)$

when $\eta \sim \xi$.

Experimentally, $\Delta \approx 60$ K,

$$\chi_{dc} \sim \exp(60/T), \quad \tau_{relax} \propto \exp((110 \div 120) / T)$$